

Discussion  
 Section,  
 week of  
 26-30 Nov  
 2018

Disc. sec. 6 (R-6?)

AM57  
 26 Nov 18

#1 R-23 relative change: ①

$$\frac{\text{new} - \text{old}}{\text{old}} = \frac{26.0 \text{ kg} - 28.1 \text{ kg}}{28.1 \text{ kg}}$$

$$= \frac{-2.1}{28.1}$$

$$= -0.075$$

$$= -7.5\%$$

on average the  
 sea otter's weight  
 has decreased by 7.5%  
 in 5 years (1.5%/year); this diff.  
 is large in practical terms

1(a)

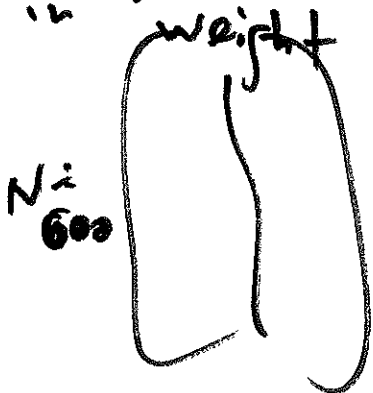
inferential summary

unk. pop. par. of main interest	$\mu = \text{pop mean weight (kg)}$
estimate of $\mu$	$\bar{y} = 26.0 \text{ kg}$
give or take for $\bar{y}$ or est. of $\mu$	$SE(\bar{y}) = 0.6 \text{ kg}$
95% CI for $\mu$	$\bar{y} \pm t_{n-1}^{0.95} \cdot SE(\bar{y}) = 26.0 \pm (2)(0.6)$

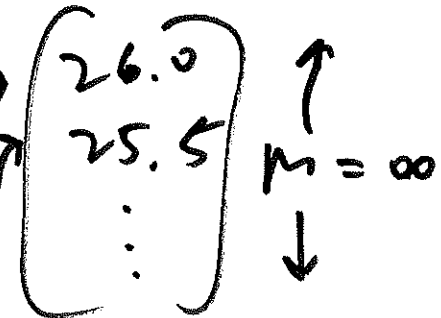
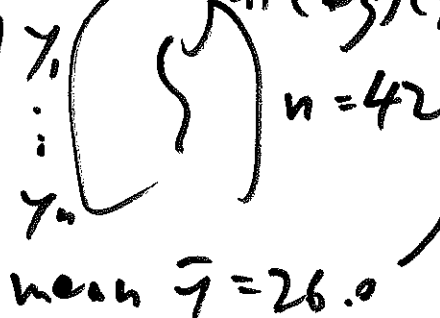
pop  
 all adult sea otters  
 E.S. (now)

sample  
 the observed sea otters (now)  
 weight (kg) ( $\bar{y}$ )

imag. data  
 all possible  $\bar{y}$  values

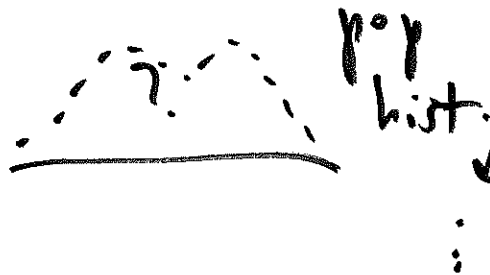
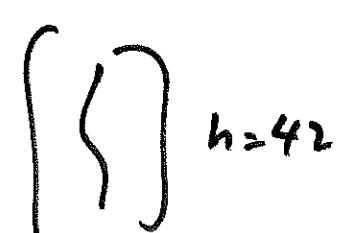


actual like IID



pop mean  $\mu = ?$   
 pop  $\sigma = ?$

hyp. IID



mean  $\bar{y} = ?$   
 (ex. 25.5)

EV of  $\bar{y}$   
 =  $\mu$

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SE of  $\bar{y}$   
 = 0.62 kg

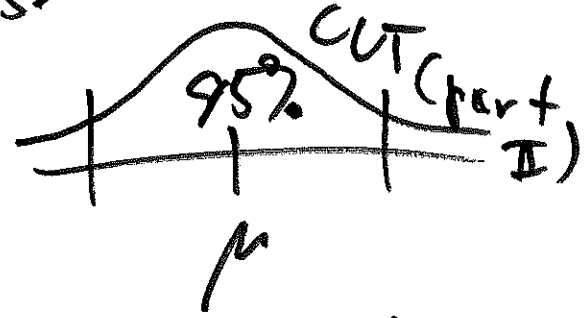
low-val. hist.

$$EV \text{ of } \bar{y} = E_{IID}(\bar{y}) = \mu \quad (2)$$

$$\hat{SE} \text{ of } \bar{y} = \hat{SE}_{IID}(\bar{y}) = \frac{4.0 \text{ kg}}{\sqrt{42}} = 0.62 \text{ kg}$$

$\hat{\sigma} = 0.6$  kg

long run



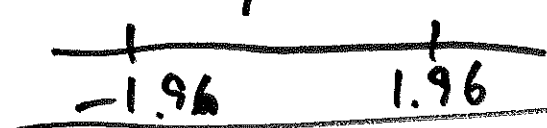
hist. of  $\bar{y}$

$L = 142$

(3)

t-table

degrees of freedom	$t^{0.95}$
40	2.021
41	2.020
45	2.014



$n = 23$  (5)

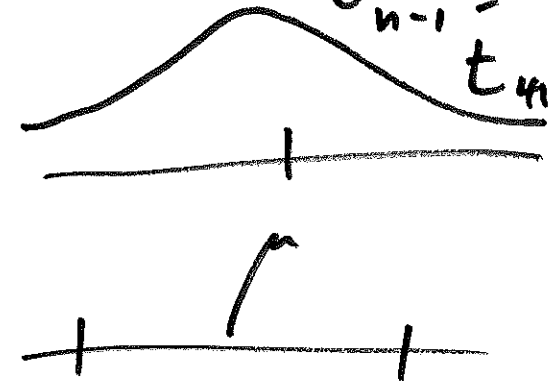
long-run

hist. of  $\bar{y}$ ,

accounting for uncertainty in  $\sigma$

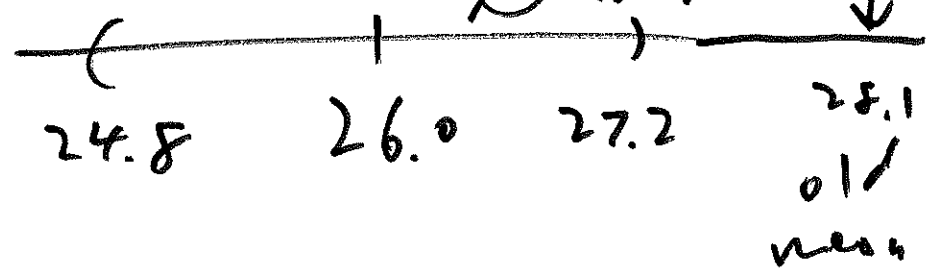
$\hat{\sigma} = 0.6$  kg

$t_{n-1} = t_{22}$



$2.02 \approx 2$

95% CI for  $\mu$  <sup>new</sup> <sub>old</sub>



Since 28.1 kg

(is) not in

the 95% CI for  $\mu$ ,

the diff. between

$\bar{y} = 26.0$  & 28.1

(is) stat sig

is probably real

is (hard) to explain by unlucky sampling

predicting the weight of a single  
randomly chosen letter from pop<sup>or sample</sup>  
161<sup>100</sup>

best ~~guess~~ prediction is  $\mu = 26.0$  kg,

give or take  $\sigma = 4.0$  kg;

so 1(b) is false; to make

or 1(c)  
1(d) true, replace 0.6 by 4.0

(empirical rule)

1(d) true	✓
1(e)	